

Generalized Cross-Ratios

Tuesday, 4 June 2024 16:00 (1 hour)

For P smooth projective variety of dim. n over \mathbb{C} complex numbers; $Y = Y_1 - Y_2$ codim r algebraic cycle, $Z = Z_1 - Z_2$ dim $r-1$ algebraic cycle, Y, Z disjoint support and homologous to 0. Biextension $B := H^{2r-1}(P \setminus (Y \cup Z), \mathbb{Q}(r))$ mixed \mathbb{Q}_{HS} with weights $0, -1, -2$ and weight graded $W_{-2}B = \mathbb{Q}(1)$, $gr_{-1}^W B = H^{2r-1}(P, \mathbb{Q}(r))$, and $gr_0^W B = \mathbb{Q}(0)$. Degenerate case $gr_{-1}^W B = (0)$ yields a Kummer extension $0 \rightarrow \mathbb{Z}(1) \rightarrow B \rightarrow \mathbb{Z}(0) \rightarrow 0$. Such a Kummer extension carries a generalized cross-ratio $\lambda(B) \in \mathbb{C}^*$. Examples and conjectures about generalized cross-ratios will be discussed.

Presenter: BLOCH, Spencer (University of Chicago)