

Explicit constructions of motivic Galois Groups

Tuesday, 11 June 2024 14:30 (1 hour)

This talk is based on the joint work with Guangyu Zhu.

The category of \mathbb{Q} -mixed Hodge-Tate structures is canonically equivalent to the category of graded comodules over a graded commutative Hopf algebra H over \mathbb{Q} . The H is isomorphic to the tensor algebra of the direct sum over $n > 0$ of $\mathbb{C}/\mathbb{Q}(n)$, placed in the degree n , with the shuffle product. However this isomorphism is not natural, and does not work in families. We give a natural explicit construction of the Hopf algebra H .

Generalizing this, we define a Hopf dg-algebra describing a dg-model of the derived category of variations of Hodge-Tate structures on a complex manifold X . Its cobar complex is a dg-model for the rational Deligne cohomology of X .

The main application is explicit construction of regulators. We define refined periods. They are single-valued, and take values in the tensor product of \mathbb{C}^* and $n - 1$ copies of \mathbb{C} . We also consider a p-adic variant of the construction.

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