

# Enriched Hodge structures and cycles on analytic thickenings

*Tuesday, 11 June 2024 16:00 (1 hour)*

This talk is a report on an ongoing project with Madhav Nori and Deepam Patel. We consider triples  $(X, A, B)$  where  $X$  is a complex analytic space,  $A, B$  are closed analytic subspaces such that  $A$  is a proper algebraic variety, and  $X \setminus B$  is a complex manifold, and  $A \setminus B$  is a submanifold. We view this as defining a representative of a germ of an analytic neighbourhood of  $A$  (the “thickening” of  $A$ ). If  $\iota : A \rightarrow X$  and  $j : X \setminus B \rightarrow X$  are the inclusions, we may consider cohomology groups  $H^m(A, \iota^*(-1)Rj_*\mathbb{Z})$  (and Tate twists). Our goal is to define a variant of Deligne-Beilinson cohomology for such objects, using Enriched Hodge structures (Bloch-Srinivas), which are “enhanced” versions of Mixed Hodge structures. We expect that our “Enriched D-B Cohomologies” would be the targets of regulators defined on suitable  $K$ -groups associated to such germs, and these would detect interesting elements in the  $K$ -theory of the germs. An example is when  $X$  is a small ball around  $A = \{0\}$  in  $\mathbb{C}^n$ , and  $B = \emptyset$ , which corresponds to the  $K$ -groups of the ring of convergent power series in  $n$  complex variables; here the underlying MHS has no information, while the “enriched” version has content. In this talk, we will indicate how the EHS’s are constructed, what the corresponding Enriched DB-cohomology looks like, and discuss some simple examples.

**Presenter:** SRINIVAS, Vasudevan (University at Buffalo)