

Computing the most stable switching laws of a linear system.

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When considering the stability under arbitrary switching of a discrete-time linear switched system $x(n+1) = A_{\sigma(n)}x(n)$, $\sigma : \mathbb{N} \rightarrow \{1, \dots, m\}$, where $x(0) \in \mathbb{R}^d$, the matrix $A_{\sigma(n)} \in \mathbb{R}^{d \times d}$ belongs to a finite family $F = \{A_i \mid 1 \leq i \leq m\}$ and σ denotes the switching law, it is known that the spectrum-minimizing product of the family F . The minimal rate of growth of its trajectories is called lower spectral radius $\hat{\rho}(F)$. For a normalized family F of matrices (i.e., with lower spectral radius $\hat{\rho}(F) = 1$) that share an invariant cone K (theorems [1, 2] and show how to generalize some of the known results to this more general setting (Guglielmi & Zennaro, in progress [5]). These generalizations are of interest because common invariant multicones may well exist when common invariant cones do not.

References

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- [3] N. Guglielmi, V.Yu. Protasov, Exact computation of joint spectral characteristics of linear operators, Found. Comput. Math., 13 (2013), pp. 37–97.
- [4] N. Guglielmi, M. Zennaro Canonical construction of polytope Barabanov norms and antinorms for sets of matrices, SIAM J. Matrix Anal. Appl. 36 (2015), pp. 634–655.
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