

Anderson acceleration with approximate least-squares calculations: applications to scientific computing

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We provide rigorous theoretical bounds for Anderson acceleration (AA) that allow efficient approximate calculations of the residual that reduce communication time and storage space while maintaining convergence. Specifically, we propose a reduced variant of AA, which consists in projecting the least squares to compute the Anderson mixing onto a subspace of reduced dimension. We numerically assess the performance of the reduced AA on: (i) linear deterministic fixed-point iterations arising from the Richardson's scheme to solve linear systems with open-source benchmark matrices with various preconditioners, (ii) non-linear deterministic fixed-point iterations arising from non-linear time-dependent Boltzmann equations, and (iii) non-linear stochastic fixed-point iterations arising from the training of neural networks. The dimensionality of the subspace onto which the least-squares to compute AA is projected adapts dynamically at each iteration as prescribed by computable quantities derived from the theoretical error bounds. The results show a reduction of the computational time without compromising the final accuracy.

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