

## Antagonistic cost functionals in shape optimization

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In several shape optimization problems one has to deal with cost functionals of the form  $\mathcal{F}(\Omega) = F(\Omega) + kG(\Omega)$ , where  $F$  and  $G$  are two shape functionals with a different monotonicity behavior and  $\Omega$  varies in the class of domains with prescribed measure. In particular, the cost functional  $\mathcal{F}(\Omega)$  is not monotone with respect to  $\Omega$  and the existence of an optimal domain in general may fail. An interesting situation occurs when the functional  $F(\Omega)$  is minimized by a ball, while the functional  $G(\Omega)$  is maximized by a ball; several examples of this kind are present in the literature. We consider the particular case  $\mathcal{F}(\Omega) = \lambda(\Omega)T^q(\Omega)$  where  $\lambda(\Omega)$  is the first eigenvalue of the Dirichlet Laplacian, and  $T(\Omega)$  is the so-called torsional rigidity; the interesting cases are  $q$  small for the minimum problem and  $q$  large for the maximum problem.

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